

# Modeling trade-offs between calcium and energy acquisition for reproducing songbirds in acidified forests

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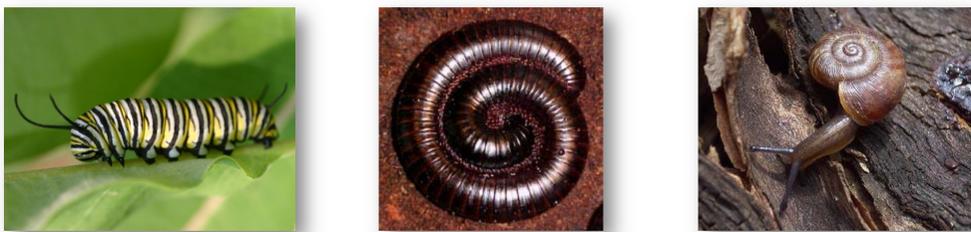
## Calcium availability can limit bird productivity and abundances in forests impacted by acid rain

- Birds require a lot of Ca to make eggshells
- Insectivorous diets do not provide enough Ca for reproduction
- Birds must supplement their diets with Ca-rich food, like snail shells
- Acid rain causes Ca to leach from soils

Acid rain → fewer snails → not enough Ca for birds → birds lay eggs with thin eggshell and lay fewer eggs

## Could a trade-off between calcium and energy acquisition explain reproductive problems in birds?

### 3 prey types



	Caterpillars	Millipedes	Snail shells
Energy (KJ/g)	6.	5.	0.5
Calcium (mg/g)	0.1	3.	90.
Handling (hrs/g)	0.0	0.035	0.10

### Optimal Foraging Theory

$$\frac{E}{T} = \frac{T_s \sum \lambda_i E_i P_i}{T_s + T_s \sum \lambda_i h_i P_i} = \frac{\sum \lambda_i E_i P_i}{1 + \sum \lambda_i h_i P_i}$$

Predator gains total energy, E (kJ), while foraging for time, T (hr) composed of time spent searching  $T_s$  (hr), and time spent handling prey,  $h_i$  (hr). Predator encounters prey  $i$  at a rate  $\lambda_i$  (g/hr), and once encountered, eats the prey with a probability of  $P_i$ . The  $i$ th prey has a net energy  $E_i$  (kJ/g), and handling time,  $h_i$  (hr).

$$\frac{E}{T} < \frac{E_b + \lambda_b E_b P_b}{T + \lambda_b h_b P_b}$$

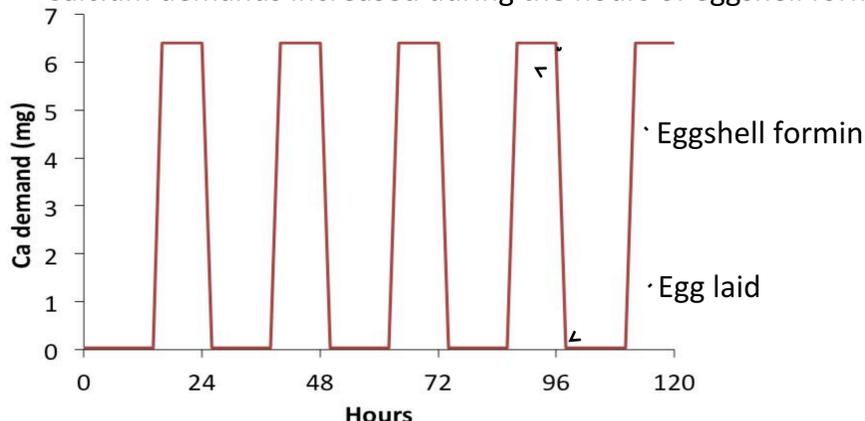
Adding a prey item, b, that does not follow the above rule will result in a decrease in the amount of energy/time that a bird gains

### Adding snails comes at the expense of energy

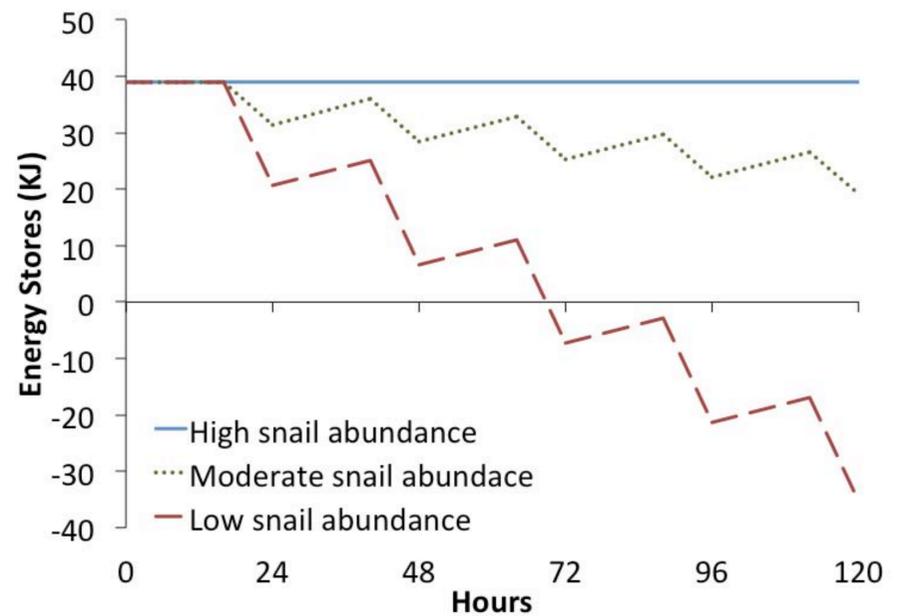
Snail shells have low energy ( $E_b$ ), high handling time ( $h_b$ ), and low availability ( $\lambda_b$ ) in acidified forests.

### Tracking E and Ca in a model bird

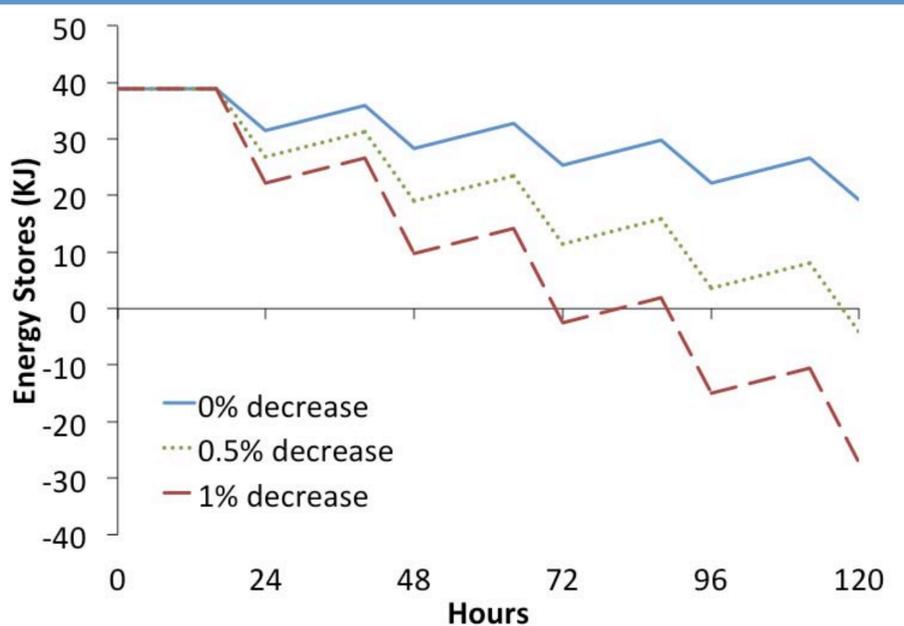
- We tracked E/T and Ca/T using the above model
- E/T was optimized under conditions that Ca demands were met
- Every 24 hours, the bird laid an egg
- The bird stored no Ca for reproduction
- The bird could store up to 39 KJ of energy (= 1 g of fat)
- Energy demand remains constant at 5.36 KJ/hour
- The eggshell is formed 8 hours before each egg is laid
- Calcium demands increased during the hours of eggshell formation



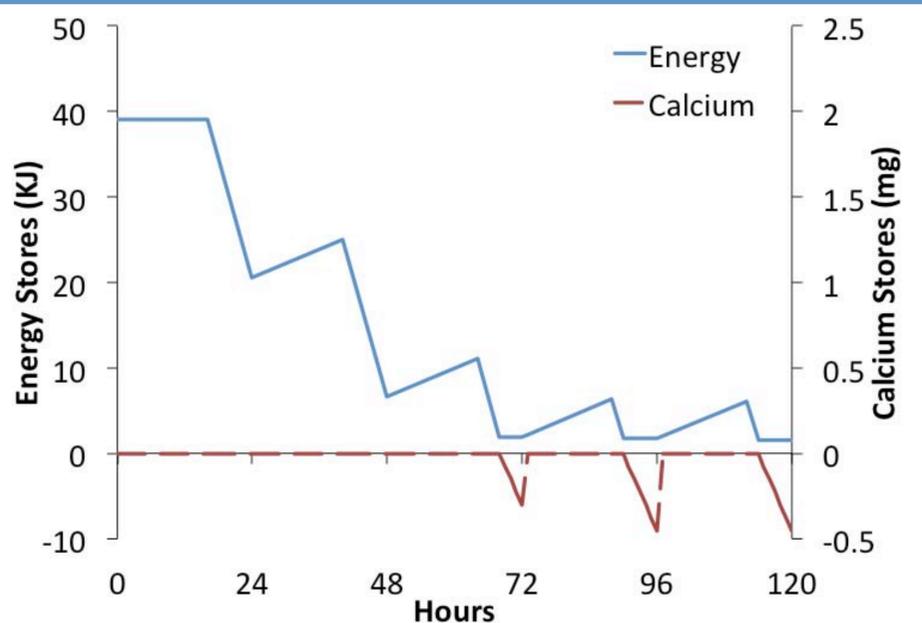
## What happens to energy stores when the encounter rate for snail shells changes?



## What happens to energy stores when the calcium content of prey changes?



## To maintain energy levels above zero, the bird can reduce calcium use by laying eggs with thin eggshells



### Conclusions

The trade-off between energy and calcium is important when calcium-rich food items have low abundances, low energy content and high handling time